

# CS480/680: Introduction to Machine Learning

## Lec 16: Contrastive Learning

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# Self-supervised Pre-training

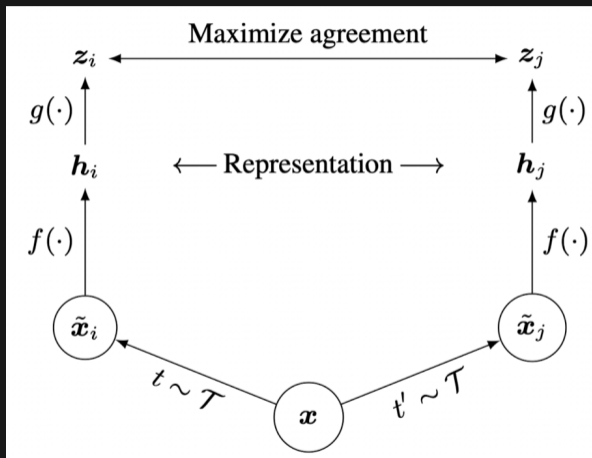
- Self-supervised pre-training of a language model by predicting the next token:

$$\min_{\Theta} \hat{\mathbb{E}} - \log \prod_{j=1}^m p(\mathbf{x}_j | \mathbf{x}_1, \dots, \mathbf{x}_{j-1}; \Theta)$$

- Self-supervised pre-training of a generative model by predicting the (next) pixel?
  - works ok for representation learning but not as competitive
  - perhaps the task of predicting the next pixel is too difficult and unnecessary

# SimCLR: Simple Contrastive Learning of visual Representation

- **Stochastic** data augmentation
- **Encoder network**  $f$  to learn representation (e.g., ResNet)
- **Projection head**  $g$  for self-supervised learning (e.g., simple 2-layer MLP)
- **Contrastive loss** to pull positive pairs and push negative pairs
  - anything but “my twin” is negative



## Algorithm 1: SimCLR

**Input:** batch size  $b$ , constant  $\tau$ , encoder  $f$ , projection  $g$ , augmentation  $\mathcal{T}$

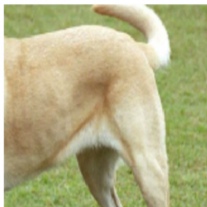
**Output:** **only** the encoder  $f$

```
1 for  $t = 0, 1, \dots$  do
2   sample a minibatch  $B_t$  with size  $b$  // large  $b$  for many negative pairs
3   for  $i = 1, \dots, b$  do
4     draw two augmentations  $T, T' \sim \mathcal{T}$ 
5      $\mathbf{z}_{2i-1} \leftarrow g(f(T(B_t[i])))$ 
6      $\mathbf{z}_{2i} \leftarrow g(f(T'(B_t[i])))$ 
7   for  $i = 1, \dots, 2b$  do
8     for  $j = 1, \dots, 2b$  do
9        $s_{ij} \leftarrow \text{sim}(\mathbf{z}_i, \mathbf{z}_j)$  // e.g.,  $\text{sim}(\mathbf{z}_i, \mathbf{z}_j) = \frac{\mathbf{z}_i \cdot \mathbf{z}_j}{\|\mathbf{z}_i\|_2 \|\mathbf{z}_j\|_2}$ , cosine similarity
10     $\min_{f,g} \frac{1}{2b} \sum_{i=1}^b \left[ -\log \frac{\exp(s_{2i-1,2i}/\tau)}{\sum_{k \neq 2i-1} \exp(s_{2i-1,k}/\tau)} - \log \frac{\exp(s_{2i,2i-1}/\tau)}{\sum_{k \neq 2i} \exp(s_{2i,k}/\tau)} \right]$ 
```

# Data Augmentation



(a) Original



(b) Crop and resize



(c) Crop, resize (and flip)



(d) Color distort. (drop)



(e) Color distort. (jitter)



(f) Rotate  $\{90^\circ, 180^\circ, 270^\circ\}$



(g) Cutout



(h) Gaussian noise



(i) Gaussian blur



(j) Sobel filtering

# Scaling

Linear probing (evaluation): fix the representation and train a linear classifier (e.g., logistic regression) on top

Self-supervised pre-training benefits from

- stronger data augmentation
- bigger (wider and deeper) models
- longer (more epochs) training
- larger batch size (more neg pairs)

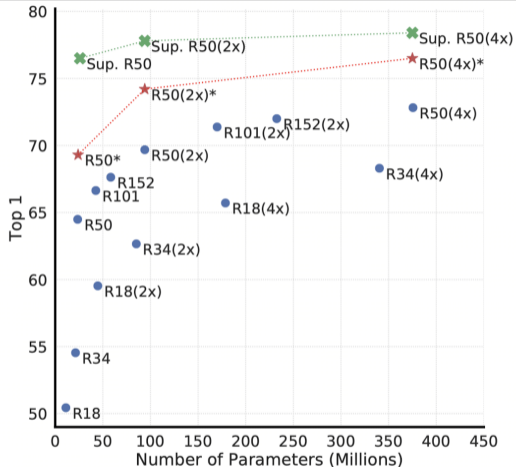


Figure 7. Linear evaluation of models with varied depth and width. Models in blue dots are ours trained for 100 epochs, models in red stars are ours trained for 1000 epochs, and models in green crosses are supervised ResNets trained for 90 epochs<sup>7</sup> (He et al., 2016).

# Projection

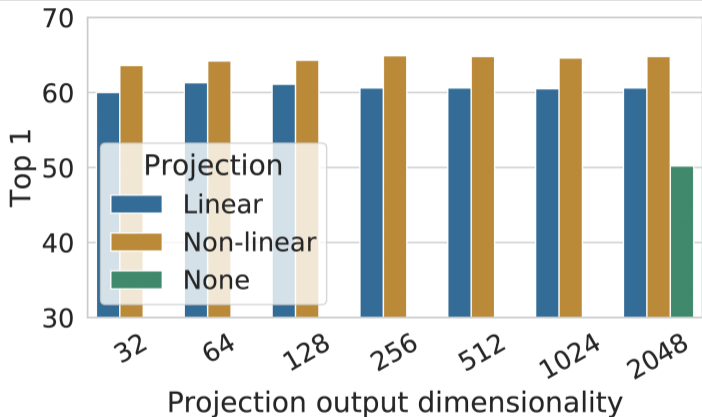


Figure 8. Linear evaluation of representations with different projection heads  $g(\cdot)$  and various dimensions of  $\mathbf{z} = g(\mathbf{h})$ . The representation  $\mathbf{h}$  (before projection) is 2048-dimensional here.

# Comparison: ResNet50(4x) vs. ResNet50

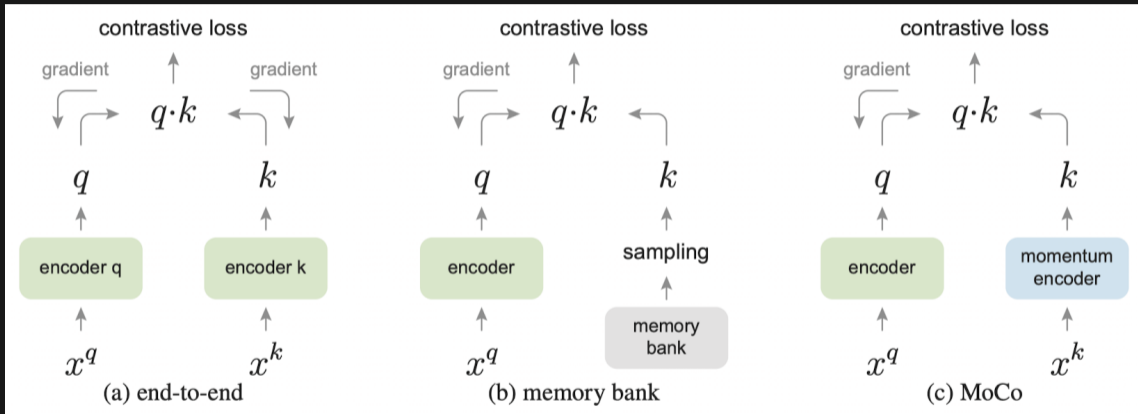
Both SimCLR and Supervised are trained on ImageNet to extract feature representation

	Food	CIFAR10	CIFAR100	Birdsnap	SUN397	Cars	Aircraft	VOC2007	DTD	Pets	Caltech-101	Flowers
<i>Linear evaluation:</i>												
SimCLR (ours)	<b>76.9</b>	<b>95.3</b>	80.2	48.4	<b>65.9</b>	60.0	61.2	<b>84.2</b>	<b>78.9</b>	89.2	<b>93.9</b>	<b>95.0</b>
Supervised	75.2	<b>95.7</b>	<b>81.2</b>	<b>56.4</b>	64.9	<b>68.8</b>	<b>63.8</b>	83.8	<b>78.7</b>	<b>92.3</b>	<b>94.1</b>	94.2
<i>Fine-tuned:</i>												
SimCLR (ours)	<b>89.4</b>	<b>98.6</b>	<b>89.0</b>	<b>78.2</b>	<b>68.1</b>	<b>92.1</b>	<b>87.0</b>	<b>86.6</b>	<b>77.8</b>	92.1	<b>94.1</b>	97.6
Supervised	88.7	98.3	<b>88.7</b>	<b>77.8</b>	67.0	91.4	<b>88.0</b>	86.5	<b>78.8</b>	<b>93.2</b>	<b>94.2</b>	<b>98.0</b>
Random init	88.3	96.0	81.9	<b>77.0</b>	53.7	91.3	84.8	69.4	64.1	82.7	72.5	92.5

	Food	CIFAR10	CIFAR100	Birdsnap	SUN397	Cars	Aircraft	VOC2007	DTD	Pets	Caltech-101	Flowers
<i>Linear evaluation:</i>												
SimCLR (ours)	68.4	90.6	71.6	37.4	58.8	50.3	50.3	80.5	<b>74.5</b>	83.6	90.3	91.2
Supervised	<b>72.3</b>	<b>93.6</b>	<b>78.3</b>	<b>53.7</b>	<b>61.9</b>	<b>66.7</b>	<b>61.0</b>	<b>82.8</b>	<b>74.9</b>	<b>91.5</b>	<b>94.5</b>	<b>94.7</b>
<i>Fine-tuned:</i>												
SimCLR (ours)	<b>88.2</b>	<b>97.7</b>	<b>85.9</b>	<b>75.9</b>	63.5	91.3	<b>88.1</b>	84.1	<b>73.2</b>	89.2	92.1	97.0
Supervised	<b>88.3</b>	<b>97.5</b>	<b>86.4</b>	<b>75.8</b>	<b>64.3</b>	<b>92.1</b>	86.0	<b>85.0</b>	<b>74.6</b>	<b>92.1</b>	<b>93.3</b>	<b>97.6</b>
Random init	86.9	95.9	80.2	<b>76.1</b>	53.6	91.4	85.9	67.3	64.8	81.5	72.6	92.0



# Moment Contrastive (MoCo)



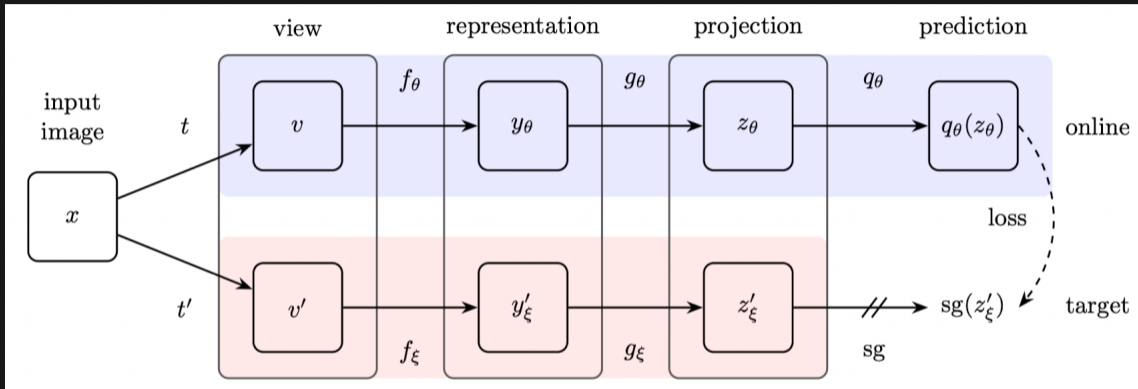
K. He et al. "Momentum contrast for unsupervised visual representation learning". In: *IEEE/CVF Conference on Computer Vision and Pattern Recognition*. 2020, pp. 9729–9738.

## Algorithm 2: MoCo

**Input:** batch size  $b$ , constant  $\tau$ ,  $d$ -dim queue for  $s$  keys, momentum  $\lambda \in [0, 1]$

```
1  $f_k = f_q$  // initialize query and key encoders
2 for  $t = 0, 1, \dots$  do
3     sample a minibatch  $B_t$  with size  $b$ 
4      $q = f_q(\text{aug}(B_t))$  // randomly augmented query
5      $k = f_k(\text{aug}(B_t))$  // randomly augmented key; detach  $k$ : no gradient to keys
6      $l_{\text{pos}} = \text{bmm}(q.\text{view}(b, 1, d), k.\text{view}(b, d, 1))$  // batch matrix multiplication
7      $l_{\text{neg}} = \text{mm}(q.\text{view}(b, d), \text{queue}.\text{view}(d, s))$  // matrix multiplication
8      $\text{logits} = \text{cat}([l_{\text{pos}}, l_{\text{neg}}], \text{dim} = 1)$  //  $b \times (s + 1)$ 
9      $\text{labels} = \text{zeros}(b)$  // positives are the 0-th
10     $\text{loss} = \text{CrossEntropyLoss}(\text{logits}/\tau, \text{labels})$  // contrastive loss
11     $\text{loss}.\text{backward}()$ 
12     $\text{update}(f_q)$  // SGD update on the query network
13     $f_k = \lambda f_k + (1 - \lambda) f_q$  // momentum update of the key network; e.g.,  $\lambda = 0.999$ 
14     $\text{enqueue}(\text{queue}, k)$  // enqueue the current minibatch
15     $\text{dequeue}(\text{queue})$  // dequeue the earliest minibatch
```

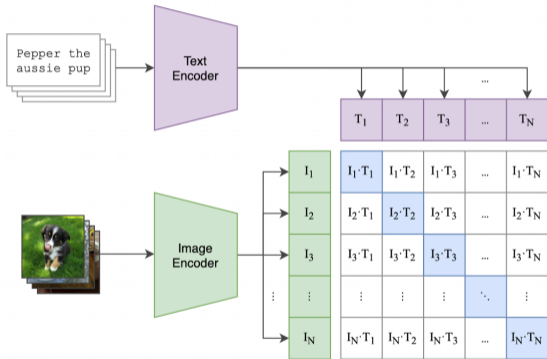
# Bootstrapping Your Own Latent (BYOL)



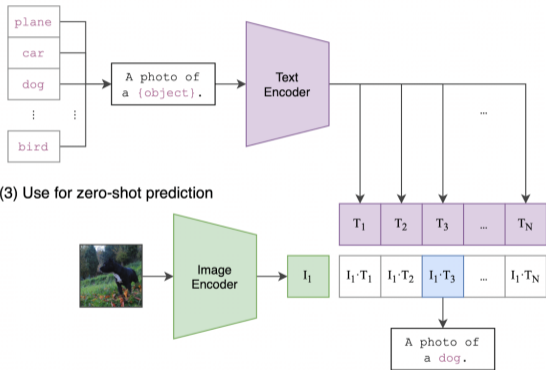
$$\min_{\theta} \text{sim}(q_{\theta}(z_{\theta}), z'_{\xi}), \quad \xi \leftarrow \lambda \xi + (1 - \lambda) \theta$$

# Contrastive Language Image Pre-training (CLIP)

## (1) Contrastive pre-training



## (2) Create dataset classifier from label text



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### Algorithm 3: CLIP

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**Input:** batch size  $b$ , temperature  $\tau$ , imageEncoder, textEncoder,  $W_i$ ,  $W_t$

```
1 for  $t = 0, 1, \dots$  do
2   sample a minibatch of images  $I_t$  and texts  $T_t$  with size  $b$ 
3    $I_f = \text{imageEncoder}(I_t)$  //  $b \times d_i$ 
4    $T_f = \text{textEncoder}(T_t)$  //  $b \times d_t$ 
5    $I_e = l2\_normalize(I_f * W_i)$  //  $W_i \in \mathbb{R}^{d_i \times d_e}$ , learned
6    $T_e = l2\_normalize(T_f * W_t)$  //  $W_t \in \mathbb{R}^{d_t \times d_e}$ , learned
7    $logits = I_e * T_e^\top * \exp(\tau)$  //  $b \times b$ 
8    $labels = [0, 1, \dots, b - 1]$ 
9    $loss_i = \text{CrossEntropyLoss}(logits, labels, axis = 0)$  // image loss
10   $loss_t = \text{CrossEntropyLoss}(logits, labels, axis = 1)$  // text loss
11   $loss = (loss_i + loss_t) / 2$  // loss to be minimized
```

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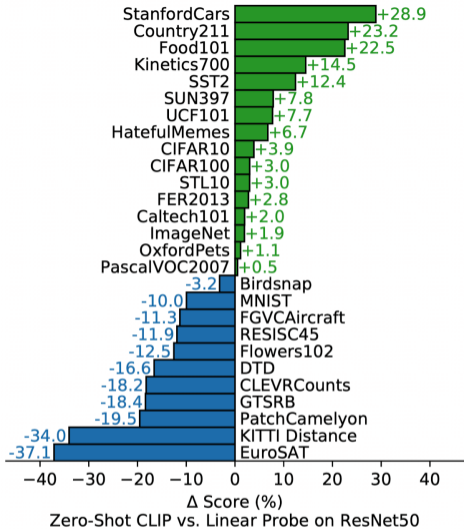
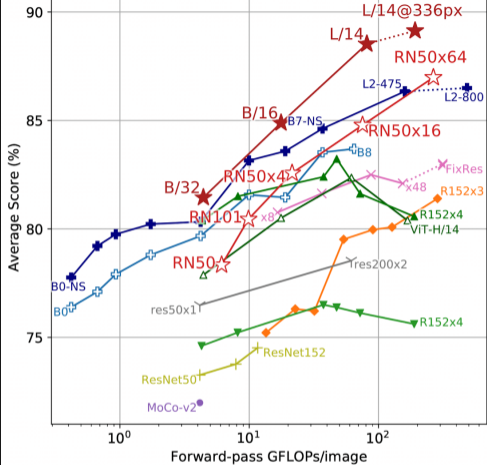
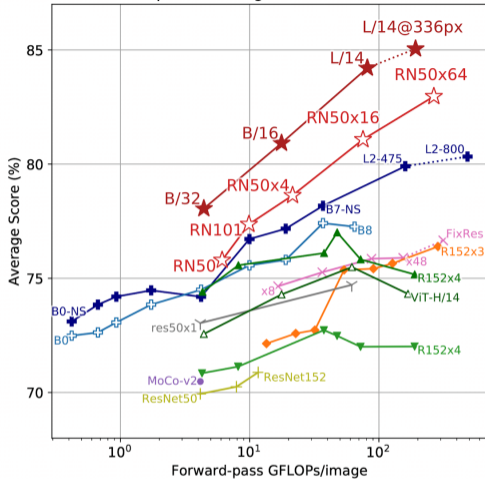


Figure 4. **Zero-shot CLIP is competitive with a fully supervised baseline.** Across a 27 dataset eval suite, a zero-shot CLIP classifier outperforms a fully supervised linear classifier fitted on ResNet50 features on 16 datasets, including ImageNet.

Linear probe average over Kornblith et al.'s 12 datasets



Linear probe average over all 27 datasets



- ★ CLIP-ViT
- ★ CLIP-ResNet
- ★ EfficientNet-NoisyStudent
- ★ EfficientNet
- ✱ Instagram-pretrained
- ◆ SimCLRv2
- ⌵ BYOL
- MoCo
- △ ViT (ImageNet-21k)
- ▲ BiT-M
- ▼ BiT-S
- + ResNet

	Dataset Examples	ImageNet ResNet101	Zero-Shot CLIP	$\Delta$ Score
ImageNet		76.2	76.2	0%
ImageNetV2		64.3	70.1	+5.8%
ImageNet-R		37.7	88.9	+51.2%
ObjectNet		32.6	72.3	+39.7%
ImageNet Sketch		25.2	60.2	+35.0%
ImageNet-A		2.7	77.1	+74.4%



# Food101

**guacamole** (90.1%) Ranked 1 out of 101 labels



✓ a photo of **guacamole**, a type of food.

✗ a photo of **ceviche**, a type of food.

✗ a photo of **edamame**, a type of food.

✗ a photo of **tuna tartare**, a type of food.

✗ a photo of **hummus**, a type of food.

# SUN397

**television studio** (90.2%) Ranked 1 out of 397 labels



✓ a photo of a **television studio**.

× a photo of a **podium indoor**.

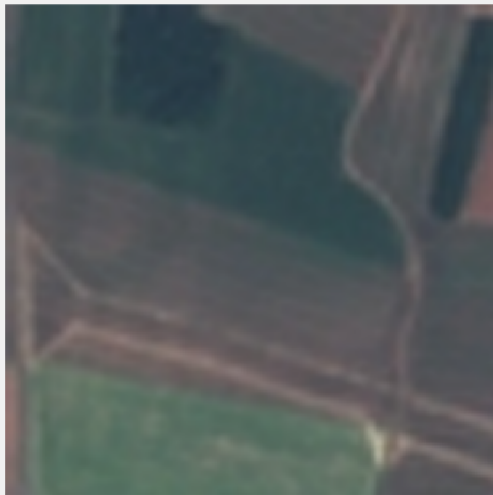
× a photo of a **conference room**.

× a photo of a **lecture room**.

× a photo of a **control room**.

# EuroSAT

**annual crop land (46.5%)** Ranked 4 out of 10 labels



a centered satellite photo of **permanent crop land**.

a centered satellite photo of **pasture land**.

a centered satellite photo of **highway or road**.

a centered satellite photo of **annual crop land**.

a centered satellite photo of **brushland or shrubland**.

## Youtube-BB

**airplane, person (89.0%)** Ranked 1 out of 23 labels



✓ a photo of a **airplane**.

✗ a photo of a **bird**.

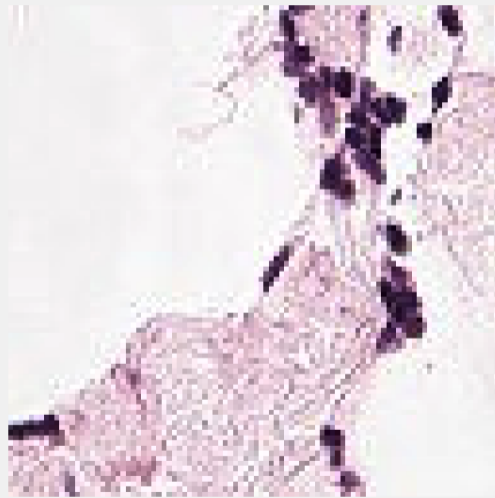
✗ a photo of a **bear**.

✗ a photo of a **giraffe**.

✗ a photo of a **car**.

## PatchCamelyon (PCam)

**healthy lymph node tissue (77.2%)** Ranked 2 out of 2 labels



× this is a photo of **lymph node tumor tissue**

✓ this is a photo of **healthy lymph node tissue**

